C2 TRIGONOMETRY — *Worksheet B*

1 Convert each angle from degrees to radians, giving your answers in terms of π.

a 180° **b** 30° **c** 45° **d** 720° **e** 18° **f** 120°

g 15° **h** 40° **i** 270° **j** 7.5° **k** 144° **l** 220°

2 Convert each angle from degrees to radians, giving your answers to 2 decimal places.

a 10° **b** 38° **c** 291° **d** 63.8° **e** 507° **f** 126.2°

3 Convert each angle from radians to degrees.

a 2π **b** $\frac{\pi}{3}$ **c** $\frac{\pi}{2}$ **d** $\frac{3\pi}{4}$ **e** $\frac{\pi}{18}$ **f** $\frac{\pi}{30}$

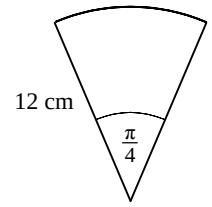
g $\frac{5\pi}{6}$ **h** $\frac{\pi}{8}$ **i** 3π **j** $\frac{2\pi}{15}$ **k** $\frac{7\pi}{3}$ **l** $\frac{9\pi}{20}$

4 Convert each angle from radians to degrees, giving your answers to 1 decimal place.

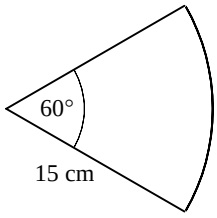
a 2^c **b** 0.5^c **c** 3.1^c **d** 1.43^c **e** 8.7^c **f** 0.742^c

5 Find, in terms of π, the length of the arc in each of the following circular sectors.

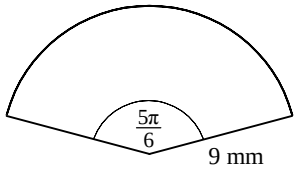
a



b

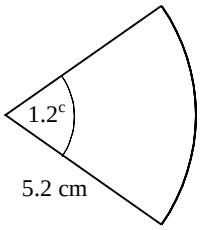


c

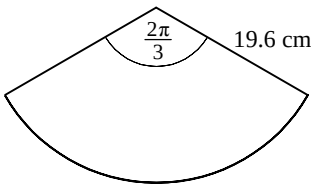


6 Find, to 3 significant figures, the perimeter of each of the following circular sectors.

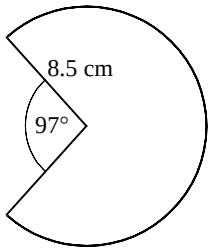
a



b

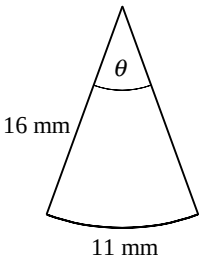


c



7 Find, in radians to 2 decimal places, the angle θ in each of the following circular sectors.

a



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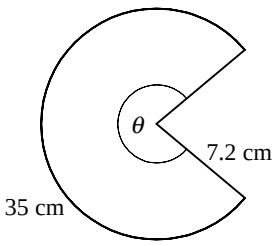

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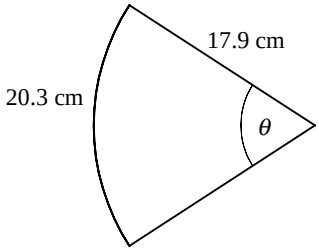


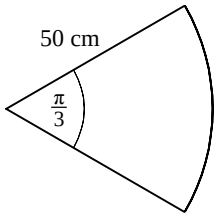
8 The minor arc AB of a circle, centre O, has length 46.2 cm.

Given that $\angle AOB = 78.5°$, find

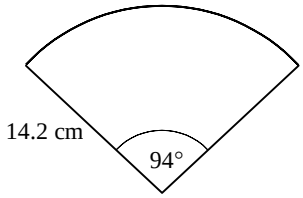
a the distance OA, **b** the perimeter of sector OAB.

9 Find, in cm^2 to 1 decimal place, the area of each of the following circular sectors.

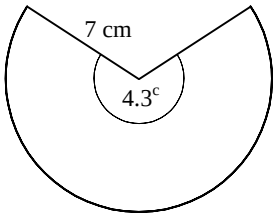
a



b



c



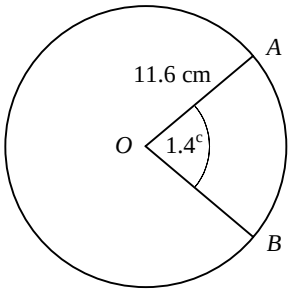
10 PQ is an arc of a circle of radius 8 cm, centre O.

Given that arc PQ has length 12 cm, find

a the angle, in radians, subtended by PQ at O,

b the area of sector OPQ.

11



The diagram shows a circle of radius 11.6 cm, centre O. The arc of the circle AB subtends an angle of 1.4 radians at O. Find, to 3 significant figures,

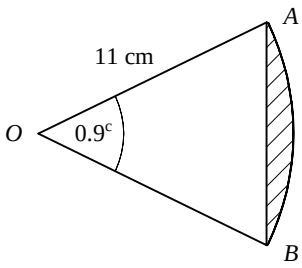
a the perimeter of the minor sector OAB,

b the perimeter of the major sector OAB,

c the area of the minor sector OAB,

d the area of the major sector OAB.

12



The diagram shows a circular sector OAB. Find the area of

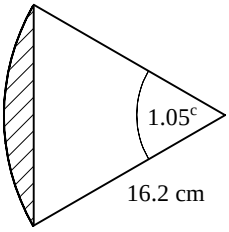
a the sector OAB,

b the triangle OAB,

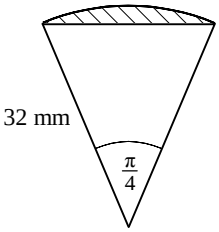
c the shaded segment.

13 Find the area of the shaded segment in each of the following circular sectors.

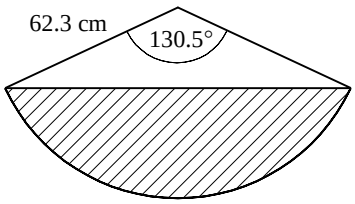
a



b



c



C2 TRIGONOMETRY — *Answers - Worksheet B*

1 **a** π **b** $\frac{\pi}{6}$ **c** $\frac{\pi}{4}$ **d** 4π **e** $\frac{\pi}{10}$ **f** $\frac{2\pi}{3}$
g $\frac{\pi}{12}$ **h** $\frac{2\pi}{9}$ **i** $\frac{3\pi}{2}$ **j** $\frac{\pi}{24}$ **k** $\frac{4\pi}{5}$ **l** $\frac{11\pi}{9}$

2 **a** 0.17^c **b** 0.66^c **c** 5.08^c **d** 1.11^c **e** 8.85^c **f** 2.20^c

3 **a** 360° **b** 60° **c** 90° **d** 135° **e** 10° **f** 6°
g 150° **h** 22.5° **i** 540° **j** 24° **k** 420° **l** 81°

4 **a** 114.6° **b** 28.6° **c** 177.6° **d** 81.9° **e** 498.5° **f** 42.5°

5 **a** $s = 12 \times \frac{\pi}{4} = 3\pi$ cm **b** $60° = \frac{\pi}{3}$
$s = 15 \times \frac{\pi}{3} = 5\pi$ cm
c $s = 9 \times \frac{5\pi}{6} = \frac{15\pi}{2}$ mm

6 **a** $P = (2 \times 5.2) + (5.2 \times 1.2)$
$= 16.6$ cm
b $P = (2 \times 19.6) + (19.6 \times \frac{2\pi}{3})$
$= 80.3$ cm
c $360° - 97° = 263° = 4.5902^c$
$P = (2 \times 8.5) + (8.5 \times 4.5902)$
$= 56.0$ cm

7 **a** $\theta = 11 \div 16 = 0.69^c$ **b** $\theta = 35 \div 7.2 = 4.86^c$ **c** $\theta = 20.3 \div 17.9 = 1.13^c$

8 **a** $78.5° = 1.3701^c$
$OA = 46.2 \div 1.3701 = 33.7$ cm (3sf)
b $P = (2 \times OA) + 46.2 = 114$ cm (3sf)

9 **a** $A = \frac{1}{2} \times 50^2 \times \frac{\pi}{3}$
$= 1309.0$ cm^2
b $94° = 1.6406^c$
$A = \frac{1}{2} \times (14.2)^2 \times 1.6406$
$= 165.4$ cm^2
c $A = \frac{1}{2} \times 7^2 \times 4.3$
$= 105.4$ cm^2

10 **a** $\theta = 12 \div 8 = 1.5^c$ **b** $A = \frac{1}{2} \times 8^2 \times 1.5 = 48$ cm^2

11 **a** $P = (2 \times 11.6) + (11.6 \times 1.4) = 39.4$ cm
b $2\pi - 1.4 = 4.8832$
$P = (2 \times 11.6) + (11.6 \times 4.8832) = 79.8$ cm
c $A = \frac{1}{2} \times (11.6)^2 \times 1.4 = 94.2$ cm^2
d $A = \frac{1}{2} \times (11.6)^2 \times 4.8832 = 329$ cm^2

12 **a** $A = \frac{1}{2} \times 11^2 \times 0.9$
$= 54.45$ cm^2
b $A = \frac{1}{2} \times 11^2 \times \sin 0.9^c$
$= 47.4$ cm^2 (3sf)
c $A = 54.45 - 47.391$
$= 7.06$ cm^2 (3sf)

13 **a** $A = [\frac{1}{2} \times (16.2)^2 \times 1.05]$
$- [\frac{1}{2} \times (16.2)^2 \times \sin 1.05^c]$
$= 137.781 - 113.823$
$= 24.0$ cm^2 (3sf)
b $A = [\frac{1}{2} \times 32^2 \times \frac{\pi}{4}]$
$- [\frac{1}{2} \times 32^2 \times \sin \frac{\pi}{4}]$
$= 402.124 - 362.039$
$= 40.1$ mm^2 (3sf)
c $130.5° = 2.2777^c$
$A = [\frac{1}{2} \times (62.3)^2 \times 2.2777]$
$- [\frac{1}{2} \times (62.3)^2 \times \sin 2.2777^c]$
$= 4420.1 - 1475.7$
$= 2940$ cm^2 (3sf)